





Supplement to Spatiotemporal Dynamics of Clusters in the Bridge Zone Linking L'Aquila 2009 and Central Italy 2016 Seismic Sequences

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The Supplement includes some sections providing additional information on clustering, key formulas to calculate the fault strength decrease by using diffusivity value, three Movies to support seismicity patterns and visualize the clusters' orientations, and eight additional Figures providing support to the main text.

1 Clustering Method

Among the various methods recently employed in seismology for the spatio-temporal clustering of seismic events, the literature includes DBSCAN (Ester et al., 1996) and HDBSCAN (Campello et al., 2013, 2015). DBSCAN and HDBSCAN have different clustering approaches, parameter sensitivity, handling of cluster shape and noise, and output management. Regarding the different approaches to the problem, DBSCAN operates a flat clustering and finds clusters simply based on density, labelling points as core, border or noise while HDBSCAN builds a hierarchy of clusters and extracts the most stable ones.

In HDBSCAN, the number of critical input parameters is reduced and robustness improved by removing the need for the radius parameter. The DBSCAN algorithm has certain shortcomings, one of which is that it cannot determine two fundamental parameters (the neighborhood of a point and the minimum number of points) by itself, and the other is that it takes a long time to traverse all points when the dataset is large (Ma et al., 2023). The radius parameter in DBSCAN defines the maximum distance between two points for them to be considered neighbors. It is a crucial parameter for determining the density of a neighborhood and is used to classify points as core, border, or noise points. Choosing an appropriate radius is critical, as a value that is too small can classify too many points as noise, while a value that is too large can merge distinct clusters. The comparison between DBSCAN

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30 and HDBSCAN reveals strengths and limitations and the choice between them depends critically on the
 31 specific application requirements and data characteristics.

32 DBSCAN and modified versions of it can offer advantages such as specificity and precision. This
 33 makes DBSCAN particularly suitable for limited blind searches and scenarios where falsely identifying
 34 non-existent clusters would be more problematic than missing some true clusters (de Berg et al., 2017).
 35 HDBSCAN's superior sensitivity of up to 82% compared to DBSCAN's 50–62% (Hunt and Reffert, 2021)
 36 makes it the stronger choice. Its ability to handle varying density environments and detect clusters
 37 across all density ranges particularly benefits analyses of heterogeneous datasets as in our case. We also
 38 preferred HDBSCAN because its parameter setup was described as easier and more intuitive, though
 39 careful parameter selection remained necessary to balance sensitivity against false positive rates (Hunt
 40 and Reffert, 2021).

41 Using silhouette score for tuning makes HDBSCAN more automated but adds complexity: instead of
 42 one parameter (minimum cluster size), a range and an evaluation metric has to be managed. We used
 43 the silhouette score to find the optimal number of clusters (higher silhouette score usually indicates
 44 better clustering). The Silhouette Coefficient is calculated using the mean intra-cluster distance (a) and
 45 the mean nearest-cluster distance (b) for each sample. It is defined as:

$$s = \frac{b - a}{\max(a, b)} \quad (1)$$

47 where:

- 48 • a is the average distance between a sample and all other points in the same cluster (intra-cluster
 49 distance).
- 50 • b is the average distance between a sample and the points in the nearest cluster that the sample is
 51 not a part of.

52 Note that the Silhouette Coefficient is only defined if the number of labels satisfies:

$$2 \leq n_{\text{labels}} \leq n_{\text{samples}} - 1 \quad (2)$$

54 In the Figure S4, we show the minimum cluster size versus the silhouette score for the time windows
 55 specified in Table 1. For finding the optimum number of clusters, we iterate the calculation of the
 56 silhouette score from 40 to 800 events with a step of 20.

57 **2 Pore Fluid Pressure Diffusion Formulas**

58 This subsection outlines the method proposed by Malagnini et al. (2010, 2012) to estimate the reduction
 59 in fault strength following a mainshock. The approach combines pore fluid pressure diffusion with

60 fault mechanical parameters to quantify how elevated fluid pressures progressively weaken the fault
 61 zone, promoting slip and cluster migration. The key components are described in Table S1.

Table S1 Model variables and their units

Symbol	Description	Units
P_f	Pore fluid pressure	Pa
P_0	Pressure at origin	Pa
P_1	Initial pressure away from origin	Pa
D	Hydraulic diffusivity	m^2/s
x	Distance from origin	m
t	Time since mainshock	s
z	Depth	m
λ_f	Pore fluid pressure coefficient	-
ρ_r	Rock density	kg/m^3
ρ_w	Fluid density	kg/m^3
g	Acceleration due to gravity	m/s^2
θ	Angle between fault and σ_1	rad
μ_s	Static friction coefficient	-
σ_n	Normal stress on fault	Pa
τ_y	Shear stress (fault strength)	Pa
z_{gt}	Gradient transition depth	m

62 For a distance x from the origin and time t , the pore fluid pressure $P_f(x, t)$ is given by:

$$63 \quad P_f(x, t) = \begin{cases} (P_0 - P_1) \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right) + P_1, & \text{steady-state,} \\ \frac{(P_0 - P_1)}{2} \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right) + P_1, & \text{non-steady-state,} \end{cases} \quad (3)$$

64 where:

$$65 \quad P_0 = \lambda_f \rho_r g z, \quad P_1 = \rho_w g z, \quad (4)$$

66 in which $\operatorname{erfc}(y) = 1 - \operatorname{erf}(y)$ is the complementary error function, $\operatorname{erf}(y)$ is the error function, and D is the
 67 hydraulic diffusivity.

68 2.1 Gradient Transition Depth

69 This subsection quantifies the depth at which the pressure gradient changes significantly, marking the
 70 transition between fluid-dominated and lithostatic regimes. The formula links pore pressure to rock
 71 density and depth, providing insight into how fluid pressure modifies effective stress conditions. Below,
 72 λ expresses the ratio of pore pressure to lithostatic pressure, and z_{gt} estimates the depth where this ratio
 73 alters stress balance.

$$74 \quad \lambda = \frac{P_f}{\rho_r g z}, \quad z_{gt} = \frac{\rho_r z (1 - \lambda)}{\rho_r - \rho_w}. \quad (5)$$

75 2.2 Fault Stress Components

76 This subsection calculates the normal stress acting on faults of different types (normal, thrust, strike-
77 slip) as a function of depth, fault orientation, and density contrast. These stresses are critical for eval-
78 uating fault strength reduction under elevated pore pressure. Finally, shear stress (fault strength) ex-
79 presses how frictional resistance scales with normal stress, which is reduced when pore pressure in-
80 creases.

Normal fault:

$$81 \quad \sigma_n = \frac{g z (\rho_r - \rho_w) \sin \theta}{\mu_s \cos \theta + \sin \theta}. \quad (6)$$

Thrust fault:

$$82 \quad \sigma_n = \frac{g z (\rho_r - \rho_w) \cos \theta}{\cos \theta - \mu_s \sin \theta}. \quad (7)$$

Strike-slip fault:

$$83 \quad \sigma_n = \frac{g z (\rho_r - \rho_w) \sin(2\theta)}{\mu_s \cos(2\theta) + \sin(2\theta)}. \quad (8)$$

84 The shear stress (fault strength) is:

$$85 \quad \tau_y = \mu_s \sigma_n. \quad (9)$$

86 3 Movies

87 Movies are uploaded as external mp4 files. M1 and M2 illustrate the evolution of seismicity in the CSZ
88 following the two mainshocks in 2009 and 2016, respectively. Movie M3 provides insight into the orien-
89 tation of seismic clusters along the defined planes.

90 **Movie M1** – Temporal evolution of seismicity in the Campotosto Seismic Zone (CSZ) following the
91 2009 L'Aquila Earthquake (M_W 6.3, April 6, 2009). The animation consists of two synchronized panels:
92 Top Panel: Map view displaying the spatial distribution of seismic events across the CSZ. Bottom Panel:
93 Longitude–Depth cross-section illustrating the vertical distribution of events along the east-west axis.
94 Seismic events are represented as colored dots, with color encoding the time of occurrence relative to
95 the mainshock, enabling visualization of the temporal migration of seismicity.

96 **Movie M2** – Temporal evolution of seismicity in the Campotosto Seismic Zone (CSZ) following the
97 2016 Amatrice Earthquake (M_W 6.1, August 24, 2016). The animation consists of two synchronized pan-
98 els: Top Panel: Map view displaying the spatial distribution of seismic events across the CSZ. Bottom
99 Panel: Longitude–Depth cross-section illustrating the vertical distribution of events along the east-west
100 axis. Seismic events are represented as colored dots, with color encoding the time of occurrence relative
101 to the mainshock, enabling visualization of the temporal migration of seismicity.

102 **Movie M3** – Horizontal rotation in the seismogenic volume containing clustered events. The ani-
103 mation presents a horizontal rotation of the 3D volume encompassing seismic clusters, which are ge-
104 ometrically approximated by planar surfaces as shown in Figure 6. The rotation provides a dynamic
105 perspective on the spatial relationships and orientations of the clusters, enhancing the visualization of
106 their structural configuration within the crust.

107 **4 Figures**

108 Figure S1 presents the frequency–magnitude distribution of events from the three high-resolution cat-
109 alogs used. Figure S2 highlights variations in strike angles derived from focal mechanism solutions.
110 Figure S3 shows changes in seismicity rates in the CSZ, both south and north of the mainshock areas.
111 Figure S4 displays the silhouette score versus the number of clusters. Figure S5 is about unclustered
112 seismicity within selected time windows. Figure S6 represents an example of PCA analysis to deter-
113 mine the best orientation of the cluster’s plane. Figure S7 reveals short-term variations in the migration
114 behavior of small clusters during the period (2010–2016). Figure S8 reports seismic front diffusivity for
115 clusters in Figure S7.

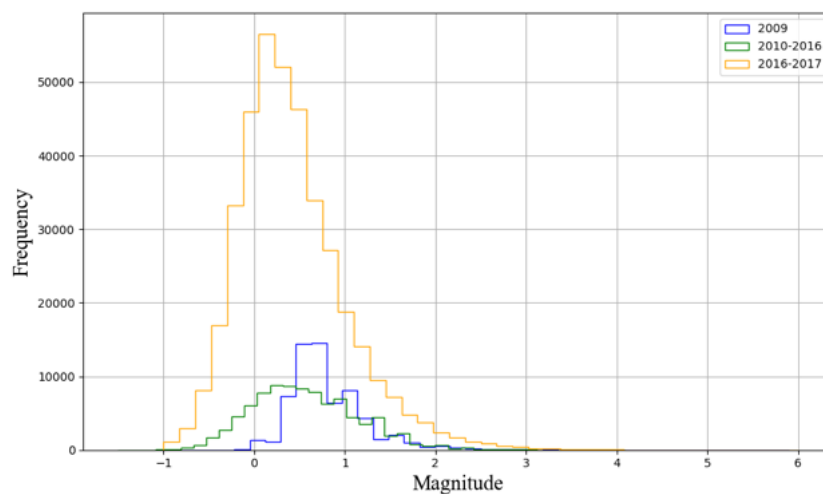


Figure S1 Magnitude–Frequency distributions from high-resolution seismic catalogs. This figure compares the magnitude–frequency distributions derived from three distinct high-resolution earthquake catalogs: (Val-
oroso et al., 2013; Sukan et al., 2023; Waldhauser et al., 2021). The distributions highlight similarities and dif-
ferences in completeness magnitude and event density across the datasets, reflecting variations in temporal
coverage, detection thresholds, and cataloging methodologies.

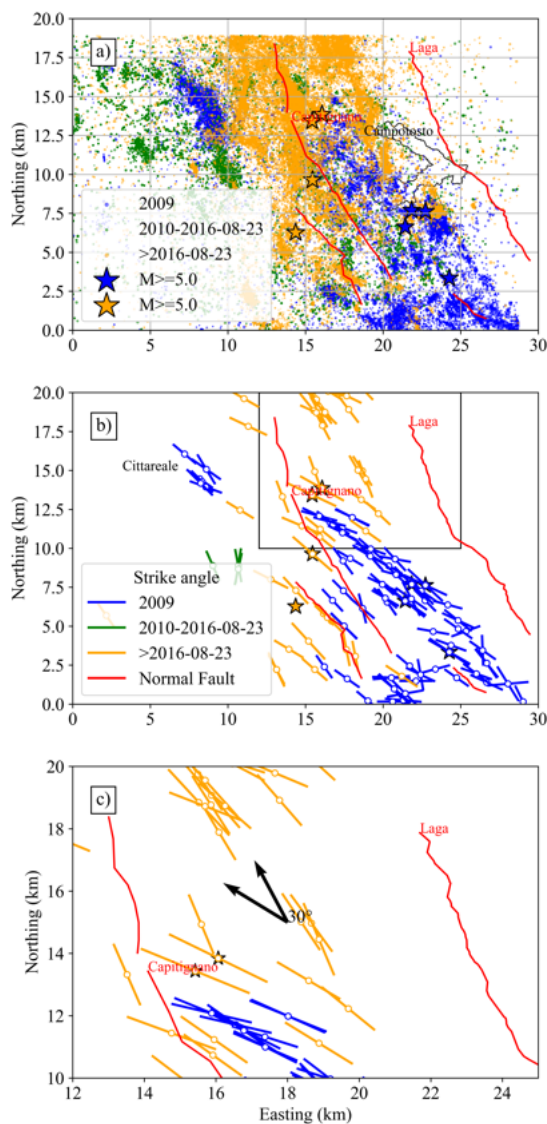


Figure S2 Seismicity and focal mechanism analysis in the CSZ (2009–2017) (a). Map view of seismicity in the Campotosto area during the 2009–2017 time window. Colored dots correspond to earthquake events from the three high-resolution catalogs listed in Table 1. (b) Strike angles of focal mechanisms for events with magnitude $M > 3$, compiled from Brennan Brunsvik et al. (2021); Locchi et al. (2024). (c) Zoomed-in view of panel (b), emphasizing the rotation in strike angles observed in the northwestern sector. Red lines indicate the surface trace of major SW-dipping normal faults, as mapped by Faure Walker et al. (2021), and serve as structural references.

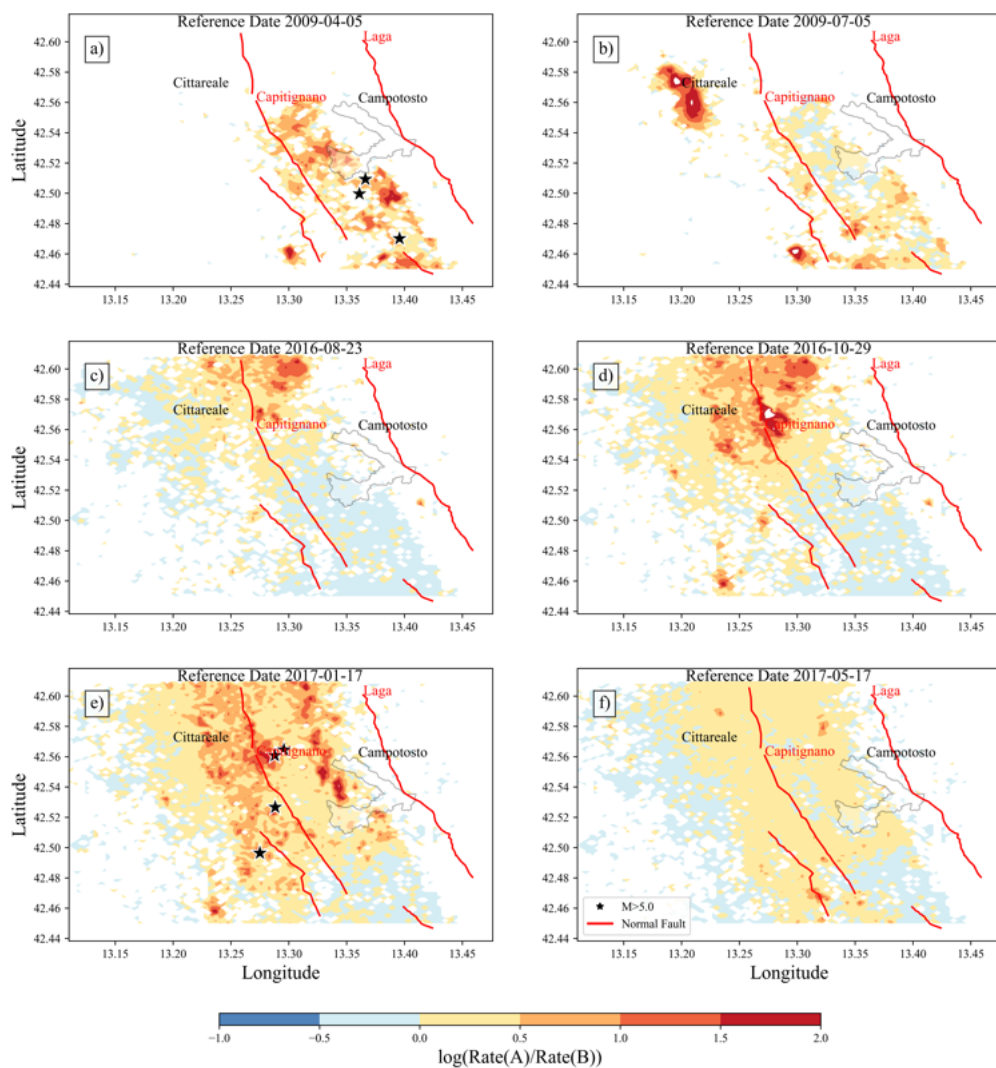


Figure S3 Seismicity rate variations in the Campotosto Seismic Zone (CSZ) across key changing point dates (0–20 km Depth Range). Seismicity rate changes are computed on a 0.3 km grid as the logarithmic ratio of event counts in two 2.5-month windows: before (B) and after (A) each reference date. Six reference dates were selected to capture major seismic transitions associated with: (a) the M_w 6.3 L’Aquila mainshock, (b) the Cittareale seismic sequence, (c) the M_w 6.1 Amatrice mainshocks, (d) the M_w 6.5 Norcia mainshock, (e) the activation of four $M_w > 5$ events within a single day, and (f) the subsequent seismic quiescence in 2017. Black stars mark events with $M_w > 5.0$. Red lines indicate the surface trace of SW-dipping normal faults (Faure Walker et al., 2021). The outline of the Campotosto water reservoir is also shown for spatial reference.

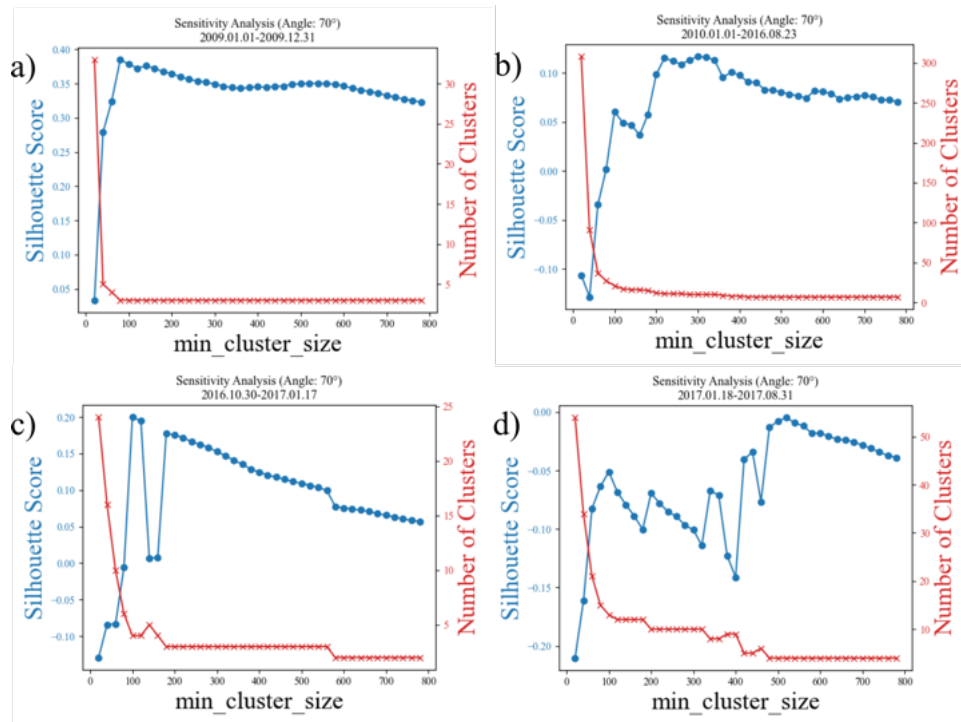


Figure S4 Minimum cluster size versus silhouette score and number of clusters for the time windows specified in Table 1.

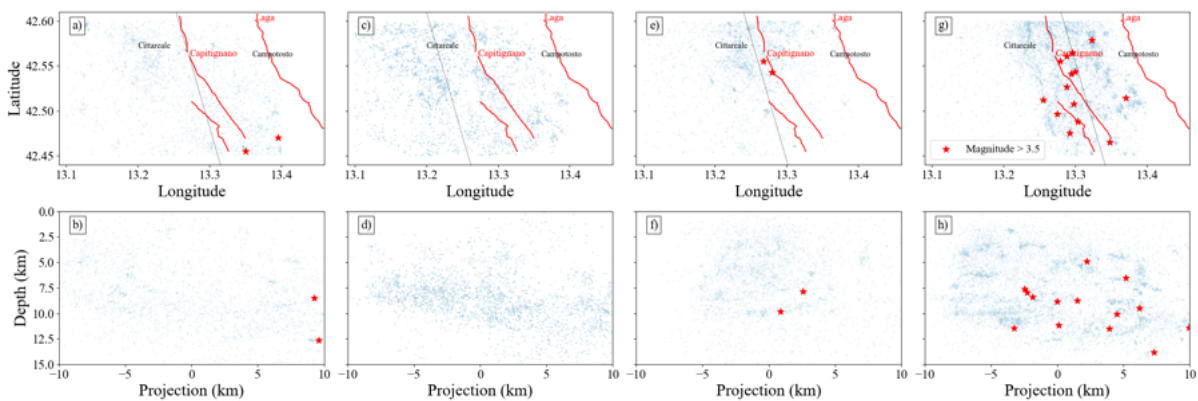


Figure S5 Residual seismicity retained after HDBSCAN cluster extraction. This figure displays the residual background seismicity in the CSZ following the removal of clustered events using the HDBSCAN algorithm. The analysis spans the same time intervals as those presented in Figure 4. The remaining events represent diffuse seismicity not associated with high-density clusters, offering insight into the spatial and temporal distribution of background activity.

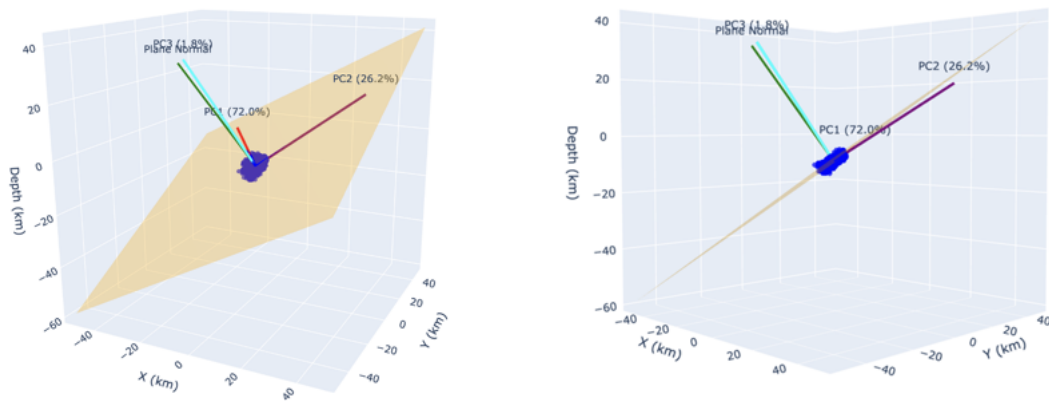


Figure S6 PCA analysis for cluster A1 to determine the plane orientation. The variance distribution along the two principal in-plane directions: approximately 72% of events align with PC1 and 28% with PC2. The third component (PC3), representing the out-of-plane direction, exhibits minimal variance.

Cluster	PC1 (%)	PC2 (%)	PC3 (%)	PC1_angle (°)
A0	50.70	36.20	13.10	99.62
A1	71.99	26.21	1.81	-35.54
A2	71.68	17.85	10.47	-33.51
C0	77.45	20.43	2.12	7.47
C1	63.39	29.81	6.80	-3.80
C2	68.21	27.28	4.51	-144.04
C3	69.25	23.67	7.08	132.66
C4	45.62	35.82	18.56	-15.45
C5	45.16	36.36	18.49	65.77
C6	65.08	29.67	5.24	-17.14
C7	59.26	28.84	11.90	132.52
C8	63.90	18.88	17.21	-63.25
C9	79.99	13.83	6.19	-22.00
E0	79.18	14.92	5.90	-5.61
E1	55.89	39.04	5.08	7.37
E2	71.32	23.56	5.12	1.65
E3	58.21	34.23	7.56	23.37
G0	68.23	17.28	14.48	10.08
G1	89.11	8.91	1.98	-20.94
G2	89.45	8.16	2.39	-21.53
G3	59.31	31.24	9.45	65.00

Table S2 Principal component percentages and PC1 orientation angle relative to North for each cluster.

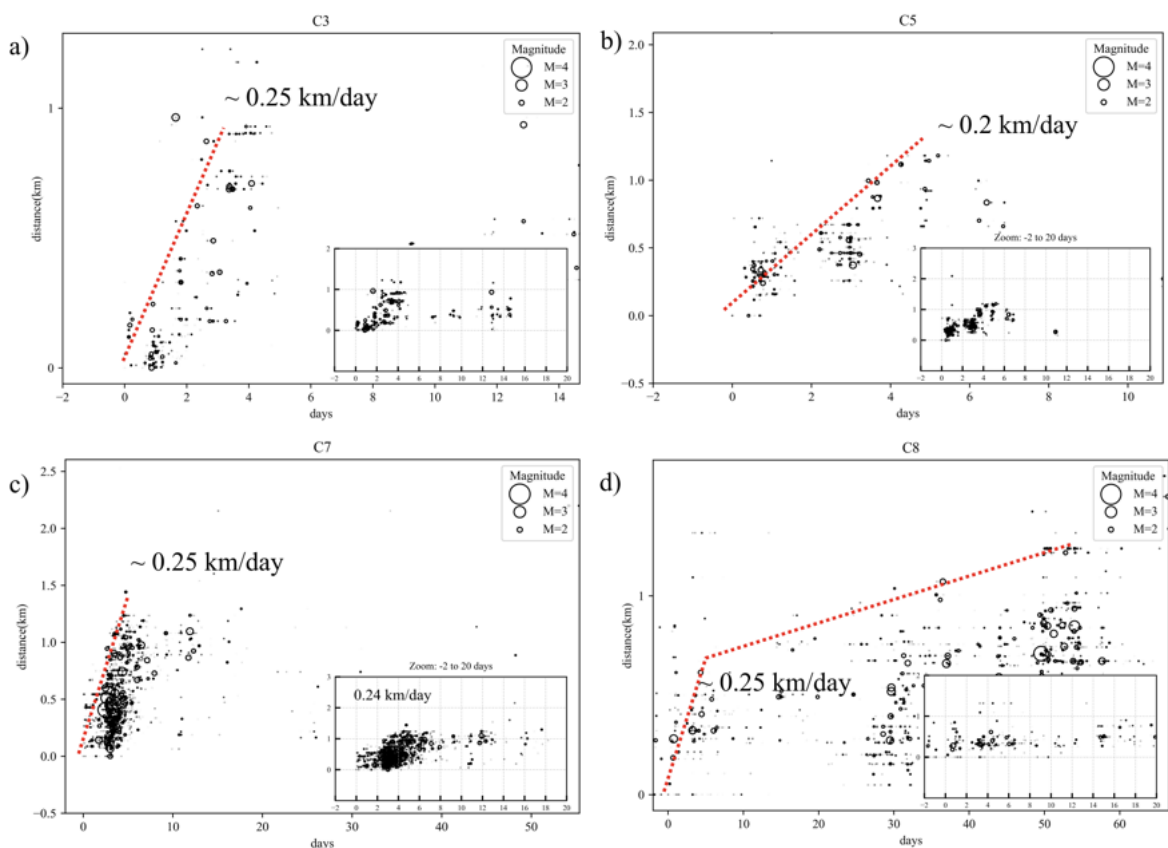


Figure S7 Seismicity front migration for clusters C3, C5, C7, and C8. Panels (a)–(d) illustrate the temporal evolution of the seismicity front for clusters C3, C5, C7, and C8, respectively. The red dotted lines represent the 90th percentile of the 3D radial distance from the initial event in each cluster, serving as a proxy for the migration velocity of seismic activity. Insets provide zoomed-in views of selected time intervals to highlight short-term fluctuations and variations in migration dynamics.

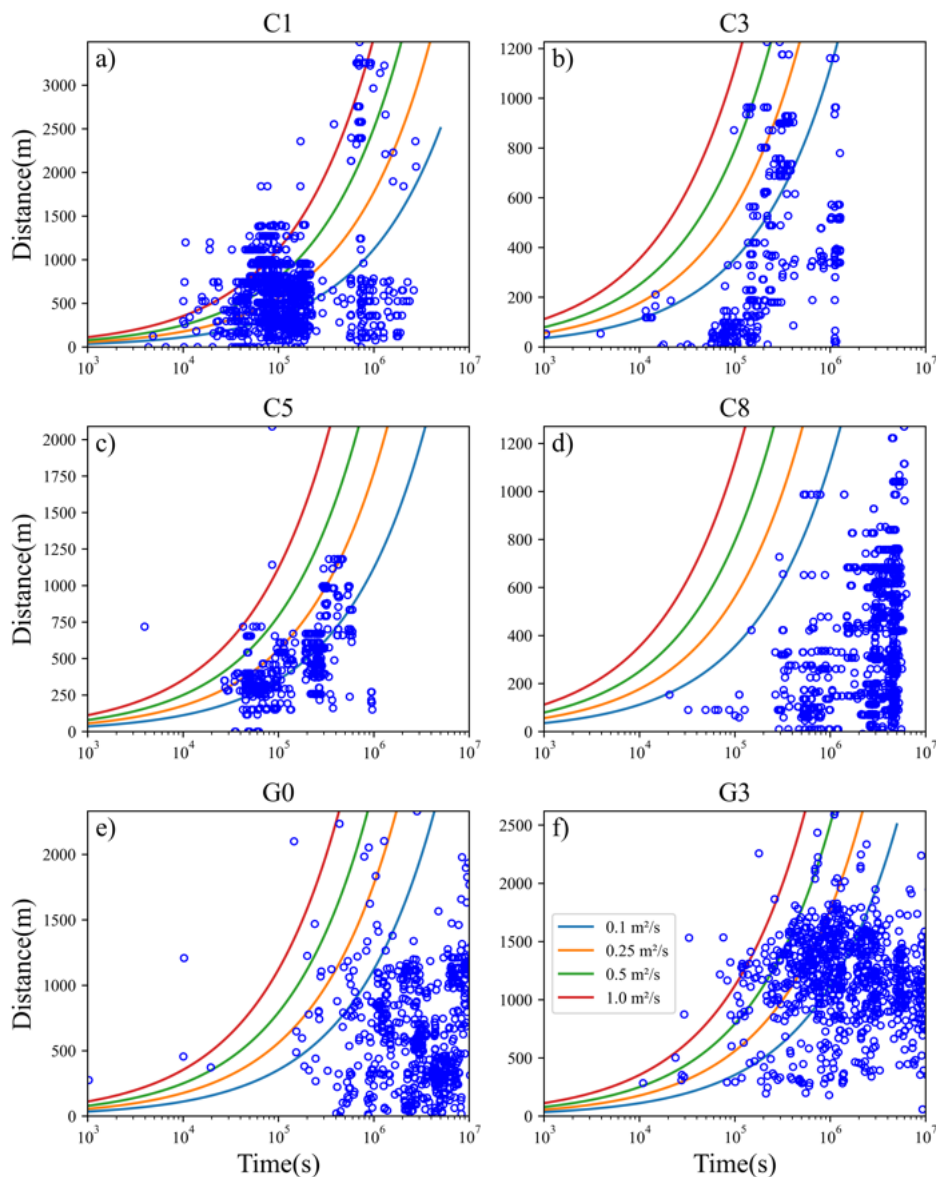


Figure S8 Diffusivity estimates for low-event-count seismic clusters This figure presents diffusivity values (D) for selected clusters characterized by a relatively small number of events, as listed in Table 1. The calculated diffusivity is generally below $1 \text{ m}^2/\text{s}$, consistent with slow migration patterns and limited spatial expansion of seismicity within these clusters.

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